

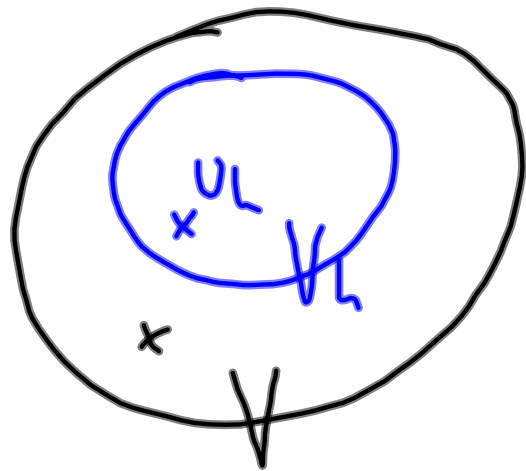
$$V_h = \{ \text{cont}, \text{cont} \rightarrow \text{cont}, \text{etc} \}$$



$$\left. \begin{array}{l} \int_{\Omega} (-\Delta u = f) \\ \int_{\Gamma_{\phi}} (\nabla u \cdot \underline{n} = \phi) \end{array} \right\} w \quad \text{w/} \quad (+)$$

$$\underbrace{\int_{\Omega} -w \Delta u - \int_{\Omega} w f}_{\text{Green}} - \underbrace{\int_{\Gamma_{\phi}} w \nabla u \cdot \underline{n} + \int_{\Gamma_{\phi}} w \phi}_{+}$$

$$\int_{\Omega} \nabla w \nabla u + \int_{\Gamma_{\phi}}$$



$$(V) \text{ Hallar } u \in V / a(u, v) = (f, v) \quad \forall v \in V$$

$$(V_h) \text{ Hallar } u_h \in \underline{V_h} / a(u_h, v) = (f, v) \quad \forall v \in \underline{V_h}$$

Alternativa:

$$(V_h) \text{ Hallar } \underline{u_h \in V_h} / \boxed{a(u_h, v) = (f, v) + \langle \phi, v \rangle} \quad \forall \underline{v \in V_h} \in \mathbb{R}$$

$$a(u_h, w) = \int_{\Omega} \nabla u_h \cdot \nabla w \, d\Omega \implies$$

$$= \int_{\Omega} \nabla \left(\underbrace{\varphi_i}_{\text{red}} \underbrace{\xi_i}_{\text{red}} + \sum_{k=M+1}^N \varphi_k \underbrace{\xi_k}_{\text{red}} \right) \cdot \nabla \varphi_j \, d\Omega$$

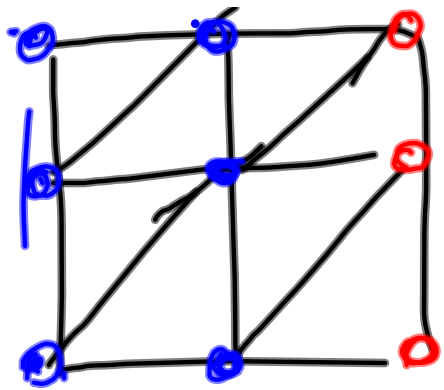
$i, j = 1, \dots, M$

$$\int \nabla \varphi_j \cdot \nabla \varphi_i \, d\Omega \xi_i + \sum_{k=M+1}^N \int \nabla \varphi_j \cdot \nabla \varphi_k \, d\Omega \xi_k$$

$$\underline{\nabla} \varphi = \begin{pmatrix} \frac{\partial \varphi}{\partial x_1} \\ \frac{\partial \varphi}{\partial x_2} \end{pmatrix}$$

$$\underline{\nabla} \varphi_i \cdot \underline{\nabla} \varphi_j = \frac{\partial \varphi_i}{\partial x_1} \frac{\partial \varphi_j}{\partial x_1} + \frac{\partial \varphi_i}{\partial x_2} \frac{\partial \varphi_j}{\partial x_2}$$

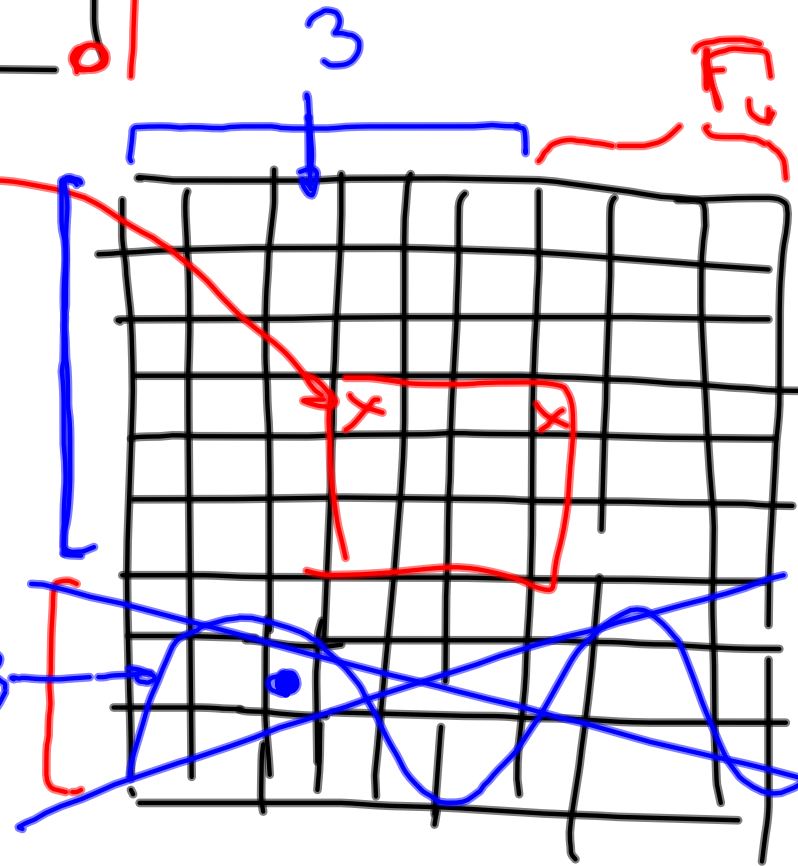
$$\Delta \varphi = \frac{\partial^2 \varphi}{\partial x_1^2} + \frac{\partial^2 \varphi}{\partial x_2^2} = \underline{\nabla} \cdot \underline{\nabla} \varphi$$



$v_h \in V_h?$

$$\mathcal{D}(v_h, v) = (f, v) \quad \forall v \in W_h$$

$$\dim(W_h) = 6$$



$$\mathcal{D}(\varphi_0, \varphi_3)$$

$$W_h = \{ \nu \text{ cont}, \nu|_K \text{ linear}, \nu = 0 \text{ on } \Gamma_U \}$$



$$\partial(\varphi_i, \varphi_k)$$

$$i = 1, M$$

$$k = M+1, N$$

$$A \begin{matrix} \text{row} \\ \text{col} \end{matrix} = \int - A_{LF} \begin{matrix} \text{row} \\ \text{col} \end{matrix}$$

$\{row, col, sk\}$

col
↓

row → []

sk

[]

$$n_{\text{global}} = (n_{\text{odo}} - 1) * n_{\text{du}} + n_{\text{cmp}}$$

Ej: $n_{\text{du}} = 2$

nodo	cmp	n_glob
1	1	1
1	2	2
2	1	3
⋮		
10	1	19